

Suppose that X and Y are independent random variables and have PMF $P(X=1)=P(Y=1)=0.1$, $P(X=2)=P(Y=2)=0.2$, $P(X=3)=P(Y=3)=0.3$, $P(X=4)=P(Y=4)=0.4$. Compute $P(X+Y \geq 7)$. Write a Matlab simulation and compare its results against your calculations.

A bit string of length 10 is sent across a lossy link. Each bit is corrupted independently with probability 0.1. What is the probability that there are at least 3 bit errors? Write a Matlab simulation and check its results against your calculations.

Consider a computer that has two operating systems installed on it. Let X and Y be the number of times the computer freezes in a day when it runs on the first and second operating systems respectively. The following reports the probability of different numbers of freezes.

	$Y=0$	$Y=1$	$Y=2$
$X=0$	0.5	0.05	0.12
$X=1$	0.10	0.07	0.01
$X=2$	0.08	0.06	0.01

Are X and Y independent? Let $Z=XY$. Find the PMF of Z .

5% of coins are not fair, with probability 0.2 of coming up heads. We toss a coin 10 times and observe less than 3 heads. What is the probability that the coin is not fair? Suppose that only 1% of coins are not fair, what is the probability now?