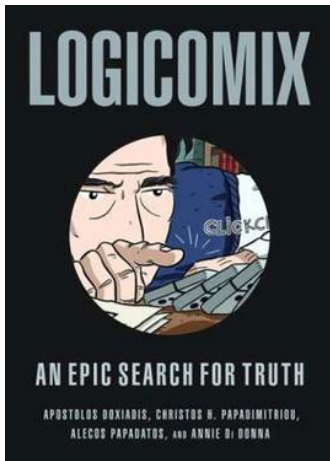


# Logic & the search for truth

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## Challenges to

- truth

Liar's Paradox: 'I am lying'

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P: *Trump is lying.*

T: *Putin is telling  
the truth.*

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$$R \in R \iff \text{not } R \in R$$

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- search (one by one)

Cantor: subsets of  $\{0, 1, 2, \dots\}$  are uncountable

$s_1 = 0$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	
$s_2 = 1$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	...
$s_3 = 0$	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	...
$s_4 = 1$	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	...
$s_5 = 1$	1	0	1	0	1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	...
$s_6 = 0$	0	1	1	0	1	1	0	1	1	0	1	1	0	1	1	0	1	1	0	1	...
$s_7 = 1$	0	0	0	1	0	0	0	1	0	0	1	0	0	1	0	0	1	0	0	1	...
$s_8 = 0$	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0	...
$s_9 = 1$	1	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	...
$s_{10} = 1$	1	0	1	1	1	0	0	1	0	1	1	0	0	1	0	1	1	0	0	1	...
$s_{11} = 1$	1	0	1	0	1	0	0	1	0	1	0	0	1	0	1	0	0	1	0	1	...
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	

$$C = \{n \mid \text{not } n \in s_n\}$$

$s = 10111010011\dots$

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  - Given a program  $P$  and data  $D$ , return either 0 or 1 depending on whether  $P$  halts on input  $D$

$$\text{HP}(P, D) := \begin{cases} 1 & \text{if } P \text{ halts on } D \\ 0 & \text{otherwise.} \end{cases}$$

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- ▶ Turing test  $\approx$  *can computers fool humans?* (CSU33061 AI 1)
  - ▶ Logic programming: *program via logic* (CSU34011)